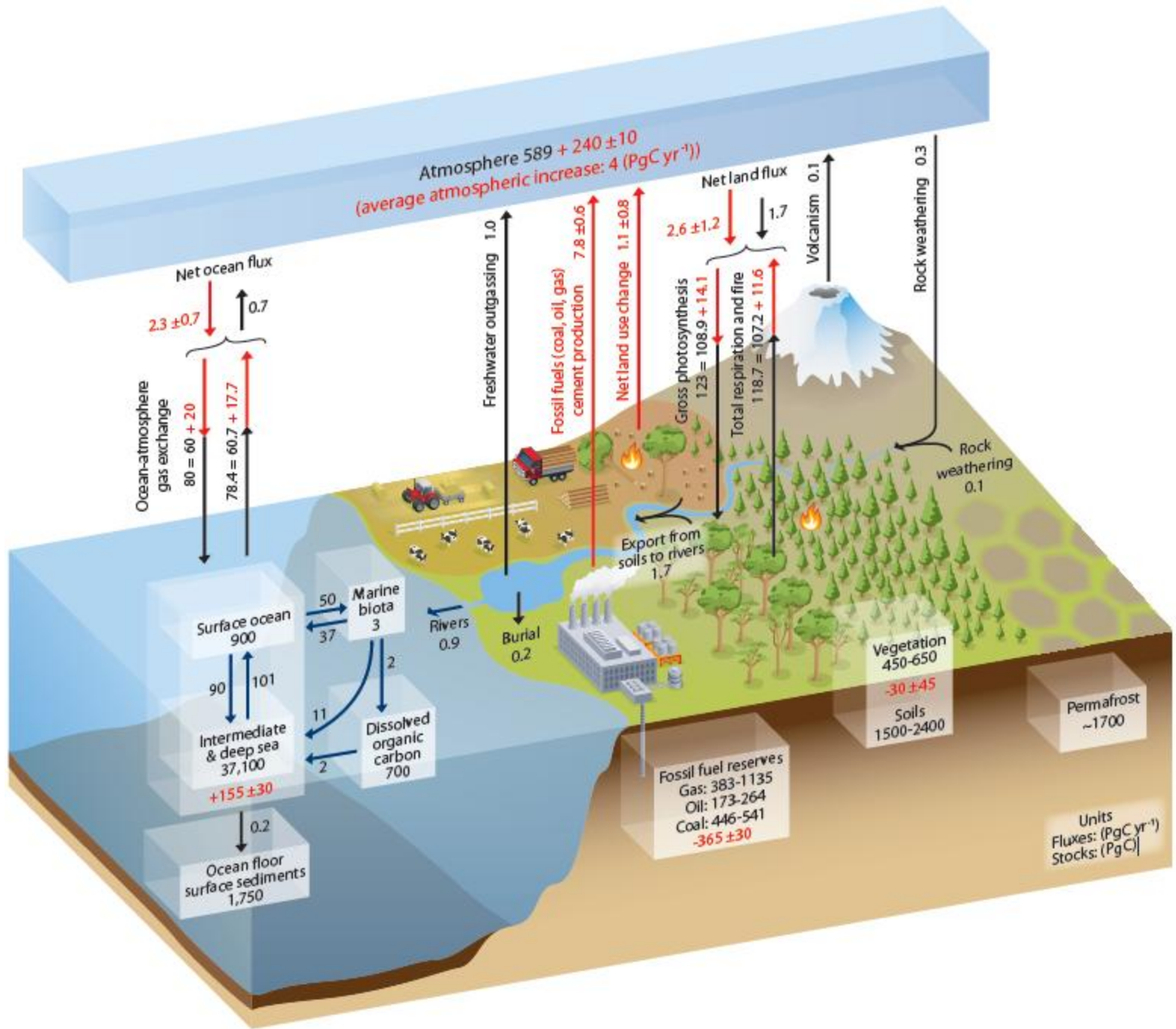


Temperature response function for soil respiration

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Temperature response functions of soil respiration (SR).

k, r, p – model parameters, T_1 – temperature ($^{\circ}C$),

$T_{ref} = 10^{\circ}C$, $T_K = 273.15^{\circ}C$, $T_0 = -46.02^{\circ}C$, $T_g = 40^{\circ}C$, $R_g = 8.31 \text{ J mol}^{-1} \text{ K}^{-1}$.

Model	Equation	Reference
1. Linear	$SR = r + k \cdot T_1$	[Wang et al., 2002; Mahadevan et al., 2008, Kur al., 2011]
2. Q ₁₀	$SR = r \cdot k^{(T_1 - T_{ref})/10}$	[van't Hoff 1898, Bond-Lamberty et al., 2011]
3. Exponential	$SR = r \cdot \exp[k \cdot T_1]$	[van't Hoff 1898, Bond-Lamberty et al., 2011]
4. Arrhenius	$SR = r \cdot \exp\left[-\frac{k}{R_g \cdot (T_1 + T_K)}\right]$	[Lloyd and Taylor, 1994; Fang and Moncrieff, 2001]
5. Lloyd&Taylor	$SR = r \cdot \exp\left[k \left(\frac{1}{T_{ref} - T_0} - \frac{1}{T_1 - T_0}\right)\right]$	[Lloyd and Taylor, 1994; Reichstein et al., 2005]
6. Power	$SR = r \cdot T_1 - p ^k$	[Fang and Moncrieff, 2001]
7. Logistic	$SR = \frac{r}{1 + p \cdot \exp[-k \cdot T_1]}$	[Richards, 1959; Rodeghiero and Cescatti, 2005]
8. Sigmoid	$SR = \frac{r}{p + k^{-(T_1 - T_{ref})/10}}$	[Jenkinson, 1990; Fang and Moncrieff, 2001]
9. Gamma	$SR = (T_1 + T_g)^r \cdot \exp[p - k \cdot (T_1 + T_g)]$	[Khomik et al., 2009; Bond-Lamberty et al., 2011]



LI-8100a - Automated Soil CO₂ Flux System with clear long-term chamber installed at Lower Observation Point (IMCES).



Bare soil site

Flux (umol/m2/s): 7,67

Flux CV (%): 1,38

Summary View

Standard View | Header Info | Measurements | **Regression Analysis**

Print

$$C(t) = C_x + (C_o - C_x) \exp(-a(t-t_o))$$

$C_o = 432,1$

$a = 1,3297E-06$

$C_x = 1000000,0$

$t_o = 13,0$

Keep

Fit	t0(s)	Slope	SE(slope)	R2	Flux	FluxCV
Expon	13,0	1,3291	0,0110	0,9926	7,67	1,00
Linear		1,3291	0,0110	0,9926	7,67	1,00

Revert



10 iterations

Adjust Start Stop | Guidance | Debug

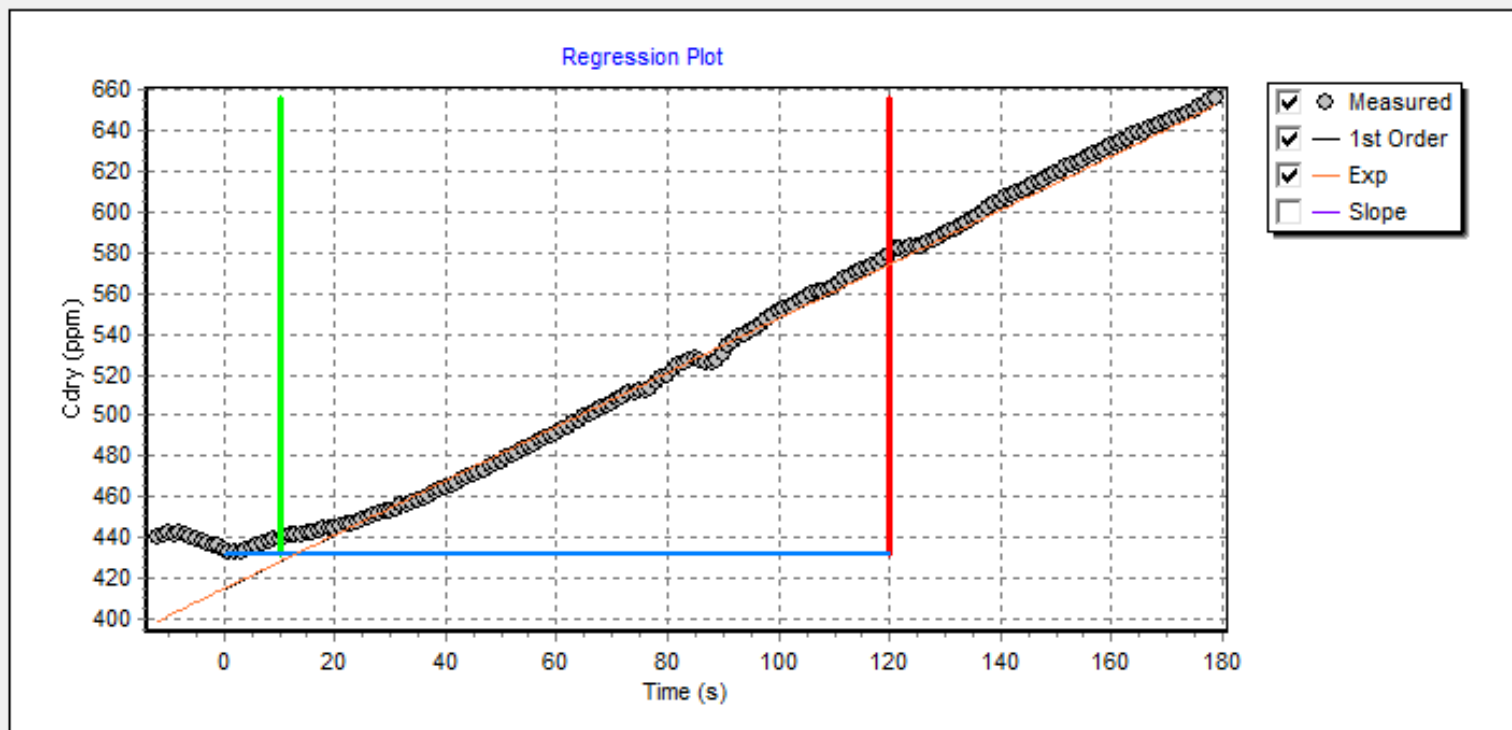
Manually Set Co

Include T<0

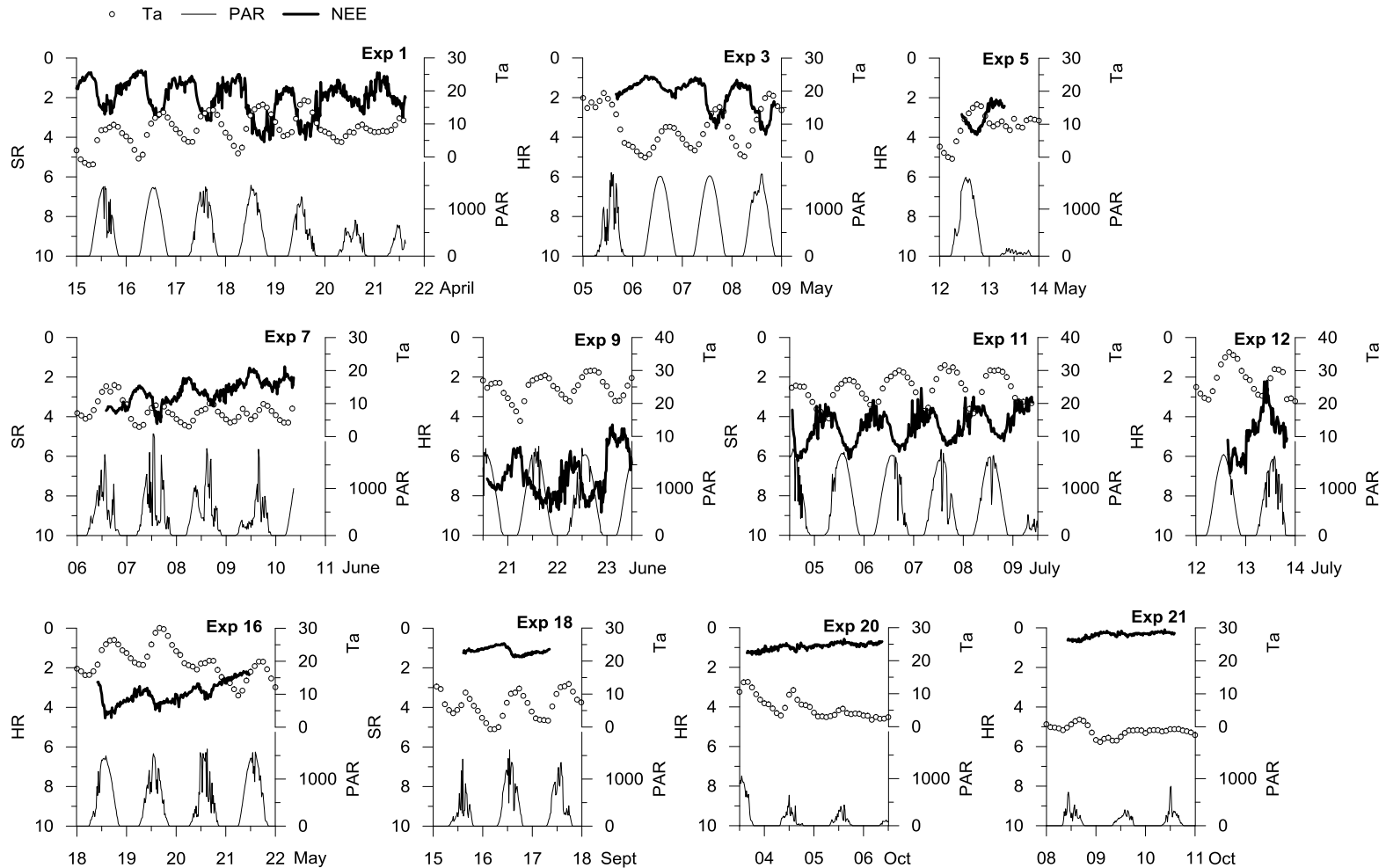
Start Time 10

Stop Time 120

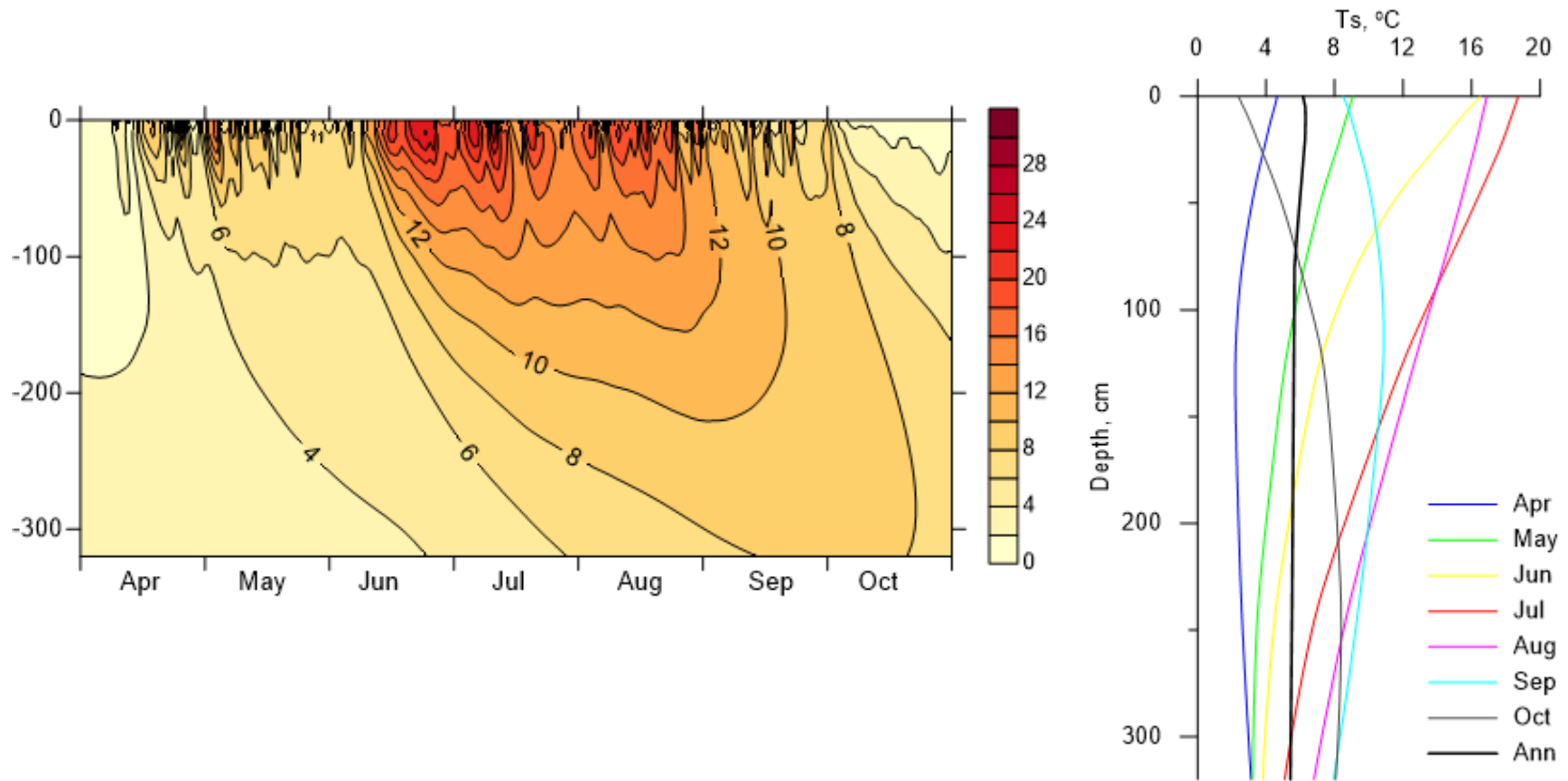
Compute



Variations of CO₂ fluxes (SR, $\mu\text{mol m}^{-2} \text{s}^{-1}$), air temperature (Ta, °C), and photosynthetically active radiation (PAR, $\mu\text{mol m}^{-2} \text{s}^{-1}$) during experiments. Note that SR axis descends.



Soil temperature



Model optimization - *fminsearch*

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (O_i - M_i)^2}$$

$$NSE = 1 - \frac{\sum_{i=1}^n (O_i - M_i)^2}{\sum_{i=1}^n (O_i - \bar{O})^2}; \quad R^2 = \left(\frac{\sum_{i=1}^n (O_i - \bar{O})(M_i - \bar{M})}{\sqrt{\sum_{i=1}^n (O_i - \bar{O})^2} \sqrt{\sum_{i=1}^n (M_i - \bar{M})^2}} \right)^2;$$

To determine the model goodness the Nash–Sutcliffe coefficient (NSE) (Nash and Sutcliffe, 1970), root mean squared error (RMSE), the coefficient of determination (R^2) were used.

O – observed, M - modelled

Temperature response functions of soil respiration (SR).

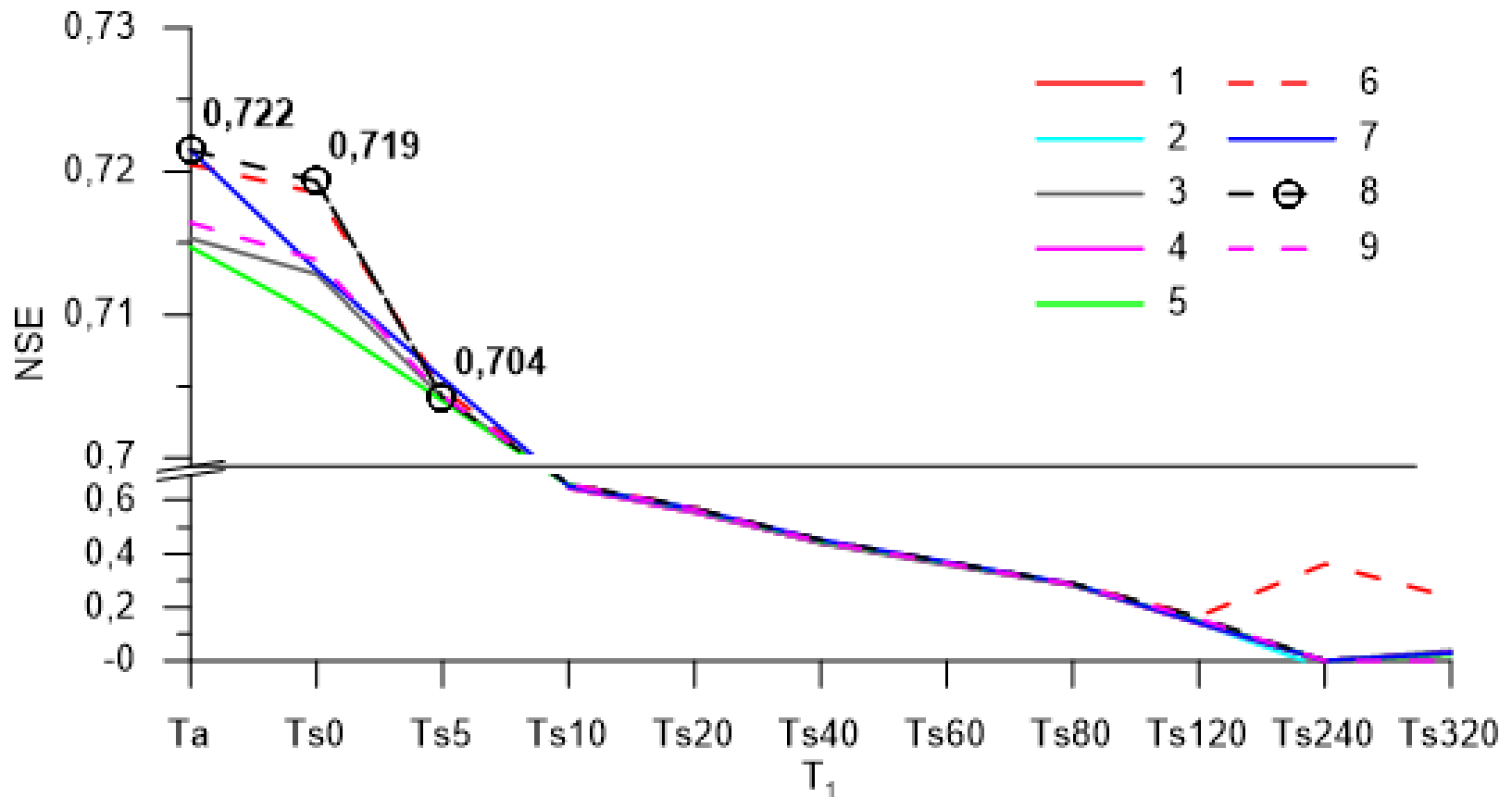
$T_{ref} = 10 \text{ }^\circ\text{C}$, $T_K = 273.15 \text{ }^\circ\text{C}$, $T_0 = -46.02 \text{ }^\circ\text{C}$, $T_g = 40 \text{ }^\circ\text{C}$, $R_g = 8.31 \text{ J mol}^{-1} \text{ K}^{-1}$.

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8. Sigmoid	$SR = \frac{r}{p + k^{-(T_1 - T_{ref})/10}}$
9. Gamma	$SR = (T_1 + T_g)^r \cdot \exp[p - k \cdot (T_1 + T_g)]$

k, r, p – model parameters

T_1 – temperature ($^\circ\text{C}$)

Controlling temperature (T_1)



6-power, 7-logistic, 8-sigmoid

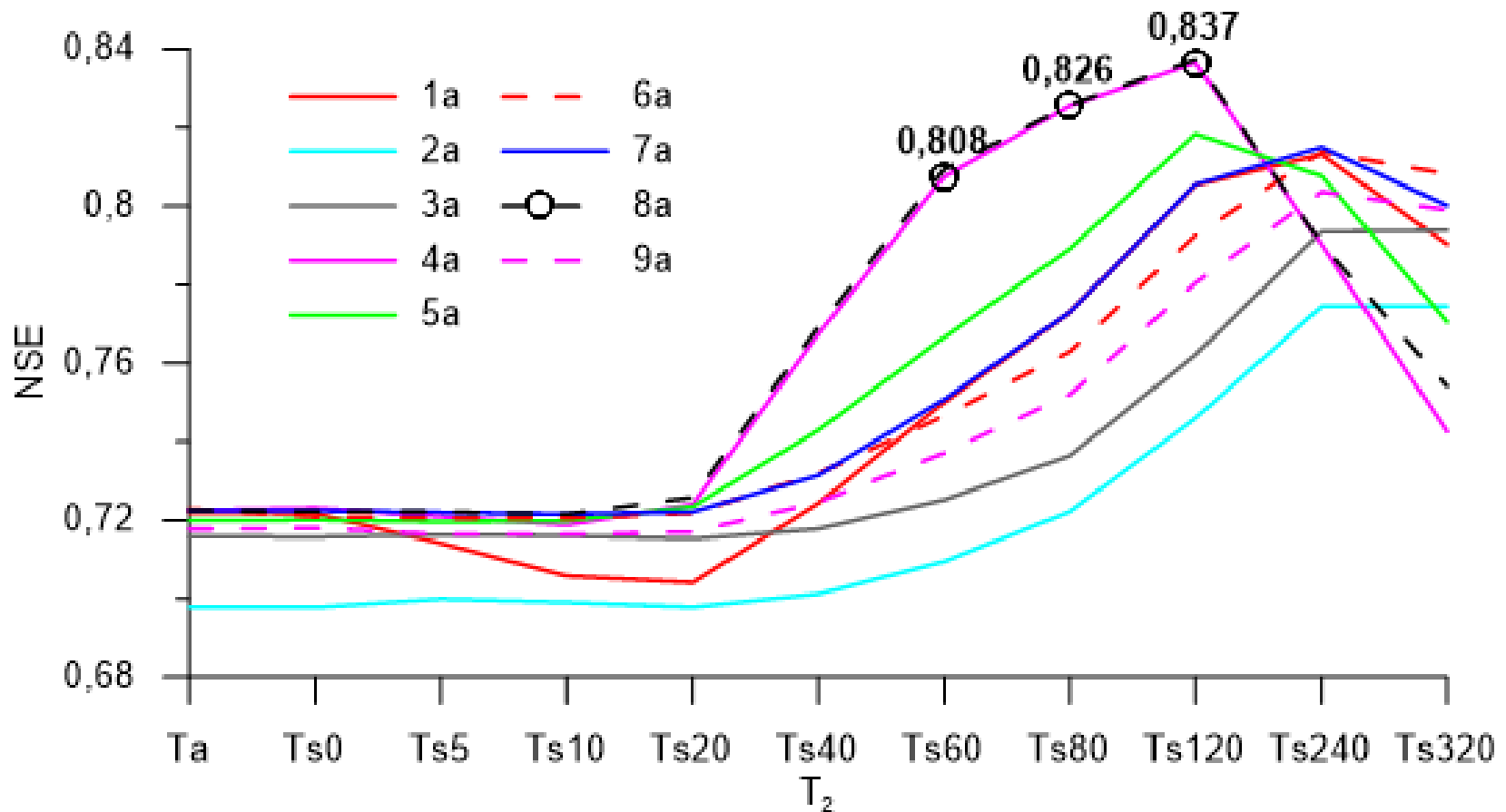
Model modification - Case A

$$k = k_0 + k_1 \cdot T_2$$

Model - 3A

$$SR = r \cdot \exp [(k_0 + k_1 \cdot T_2) \cdot T_1]$$

Controlling temperature for modification «A»



4-Arrhenius, 8-sigmoid

Model modification – case B

$$k = k_0 + k_1 \cdot T_2$$

$$r = r_0 + r_1 \cdot T_3$$

Model – 3B

$$SR = (r_0 + r_1 \cdot T_3) \cdot \exp [(k_0 + k_1 \cdot T_2) \cdot T_1]$$

Controlling temperatures for models «B» - NSE

N – depth

1 – Ta

2 - 0

3 - 5

4 - 10

5 - 20

6 - 40

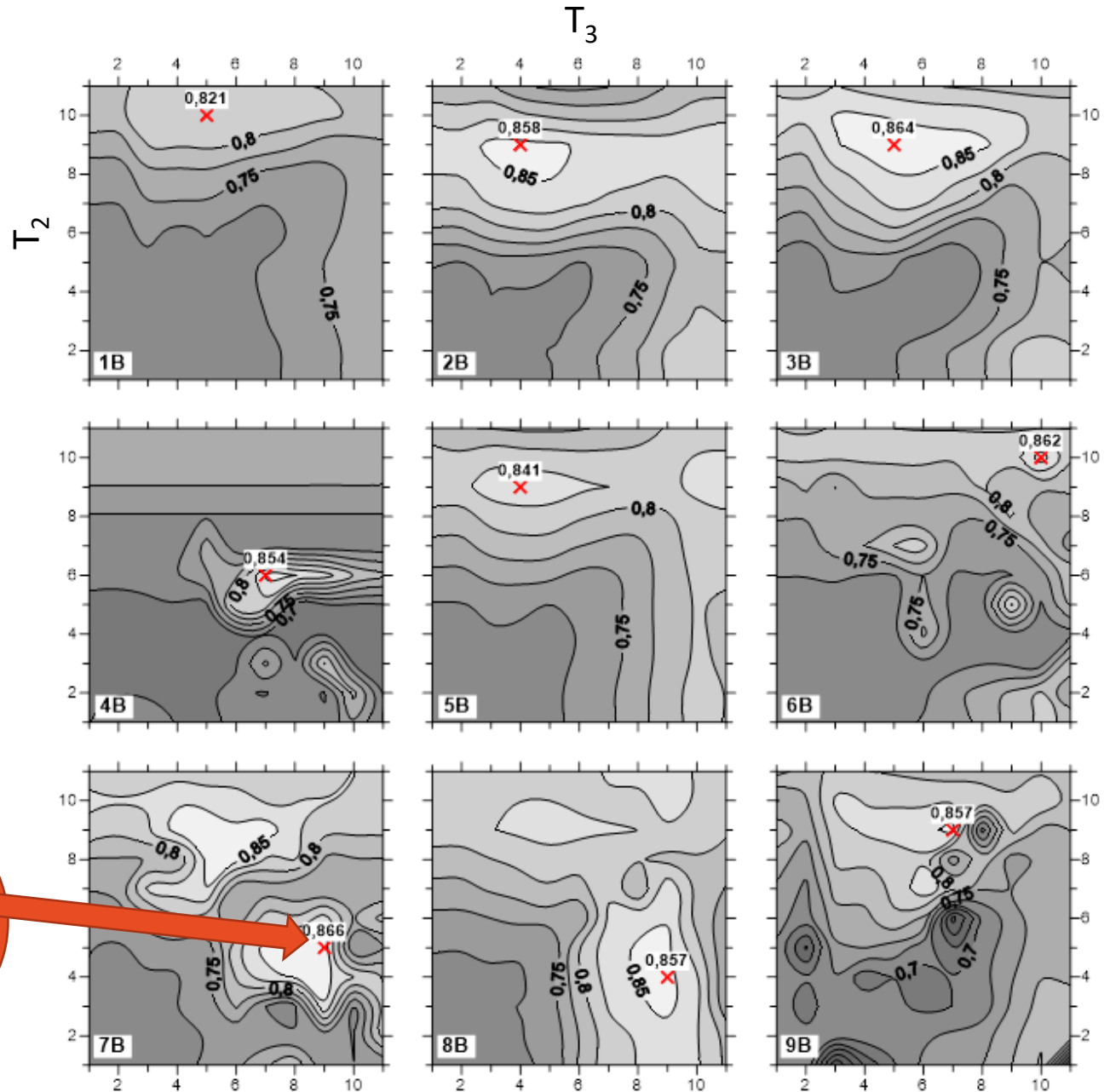
7 - 60

8 - 80

9 - 120

10 - 240

11 - 320



Model 7B

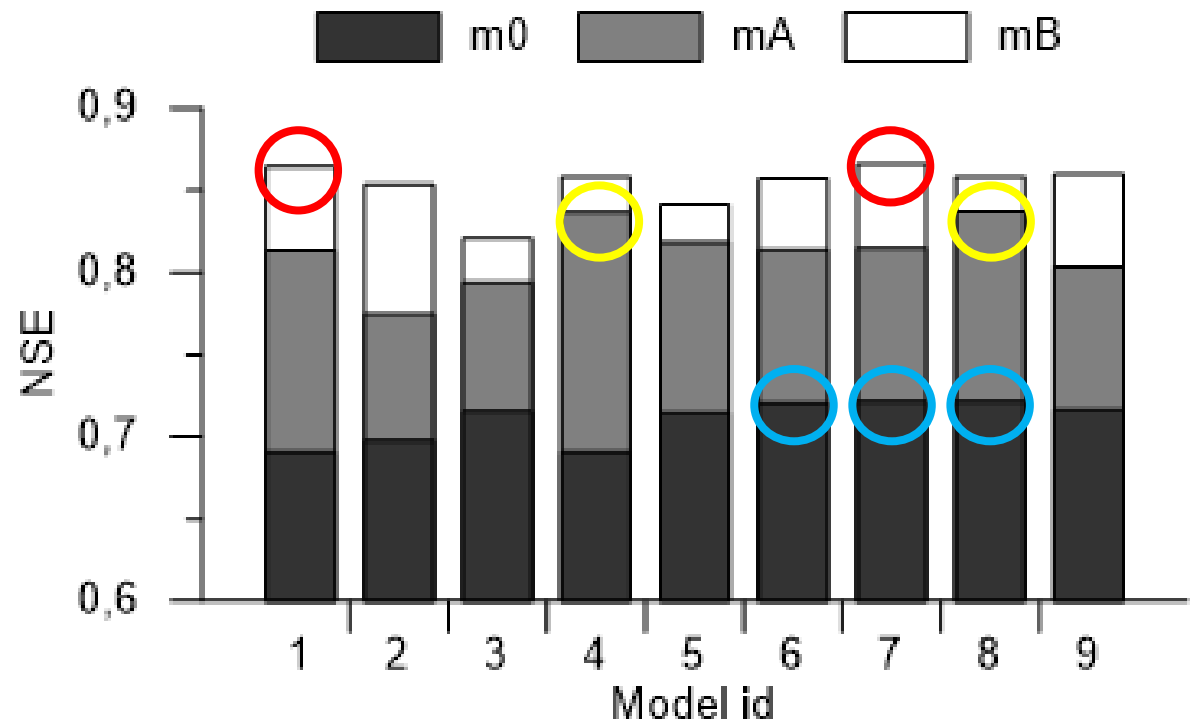
$T_1 = T_{air}$

$T_2 = T_{20}$

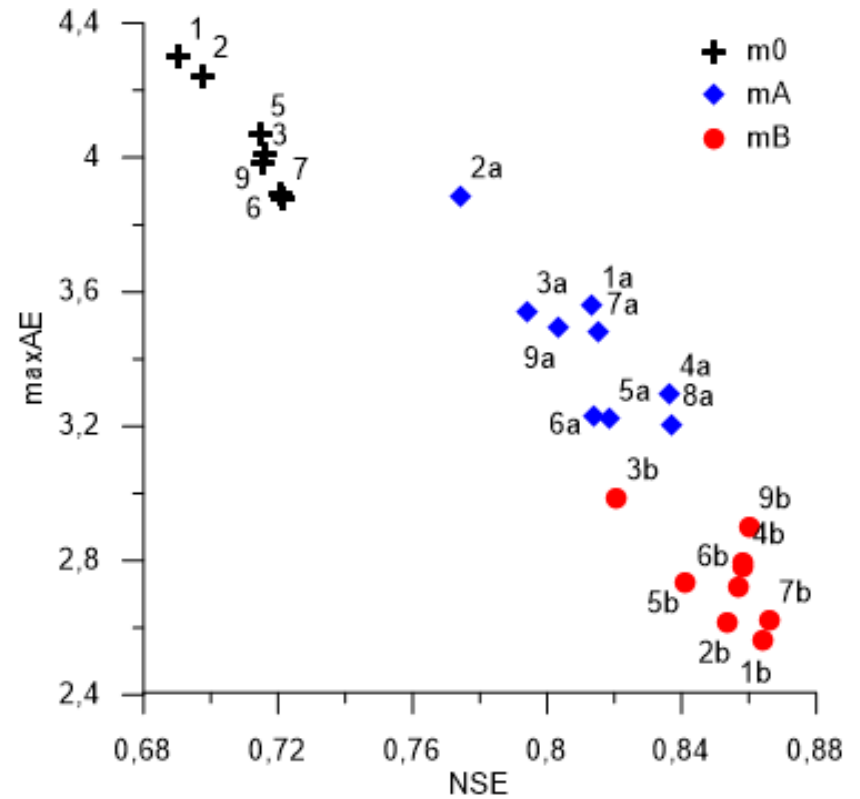
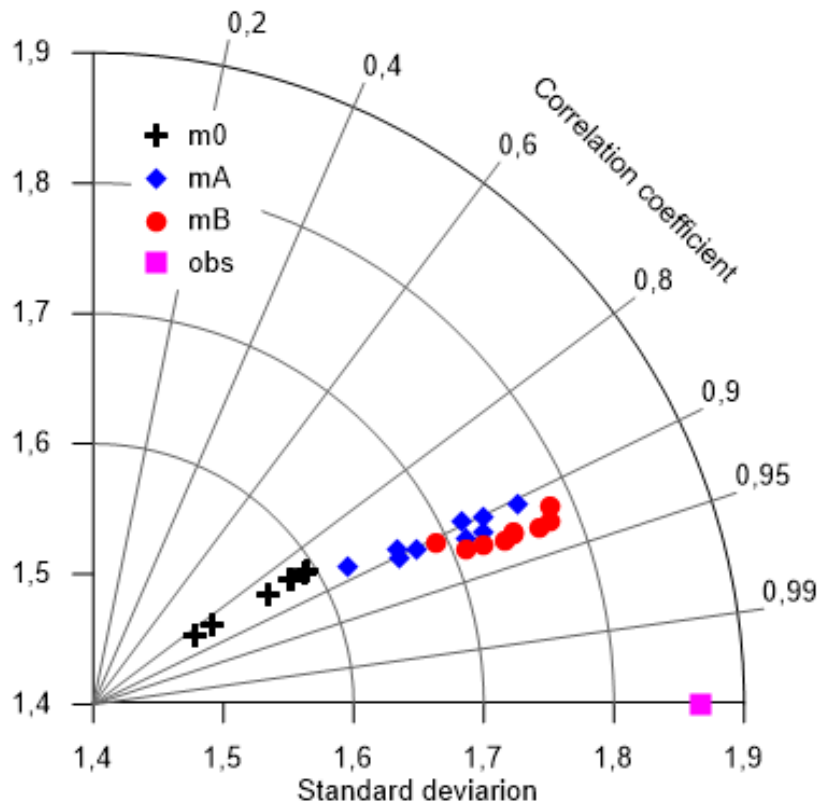
$T_3 = T_{120}$

Model performance comparison

- 1. Linear
- 2. Q10
- 3. Exponential
- 4. Arrhenius
- 5. Lloyd&Taylor
- 6. Power
- 7. Logistic
- 8. Sigmoid
- 9. Gamma

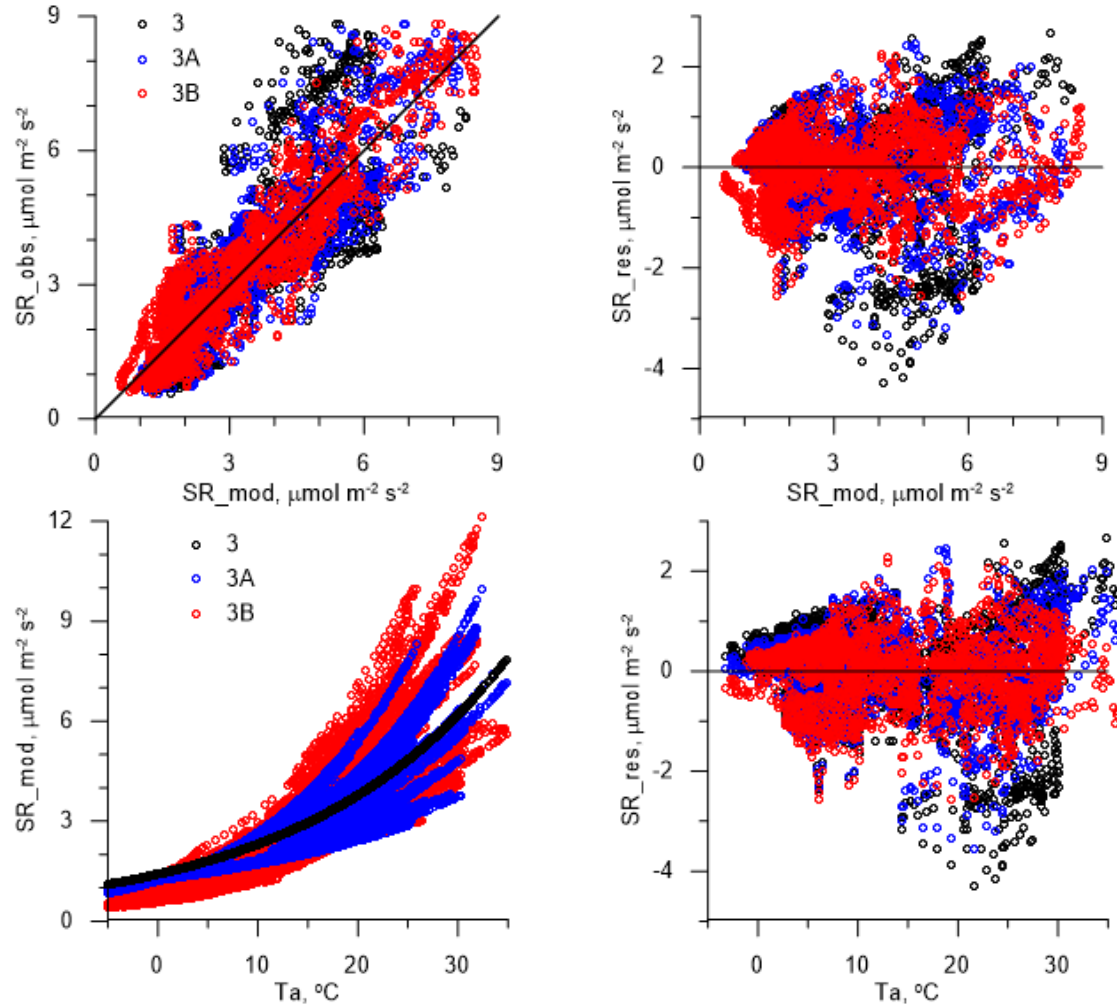


Model performance comparison



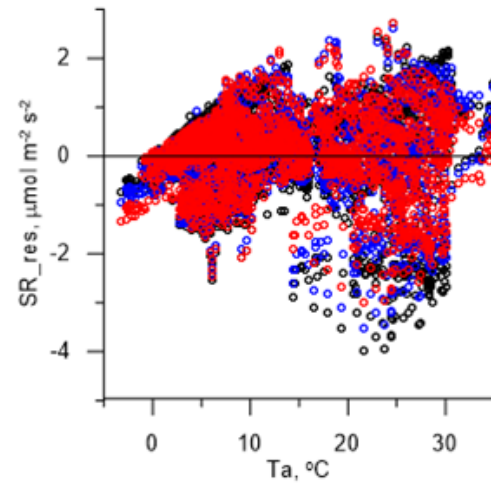
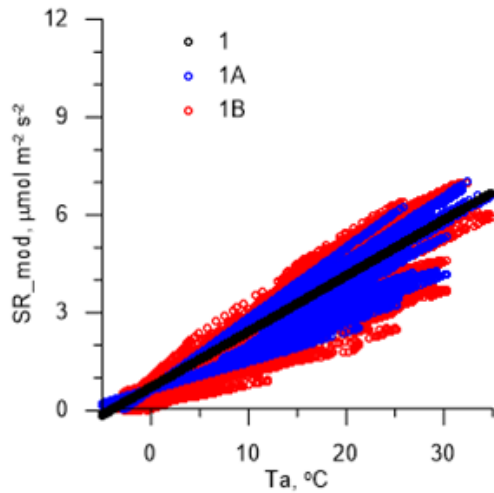
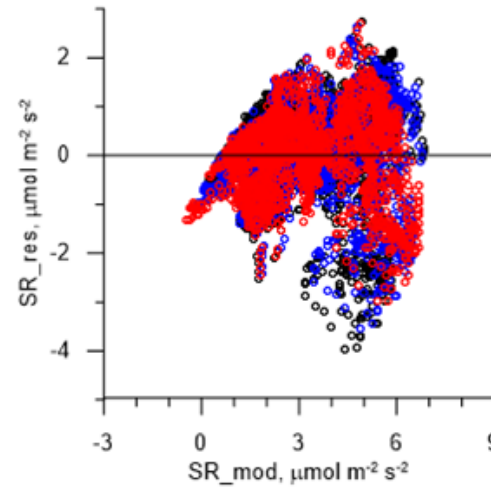
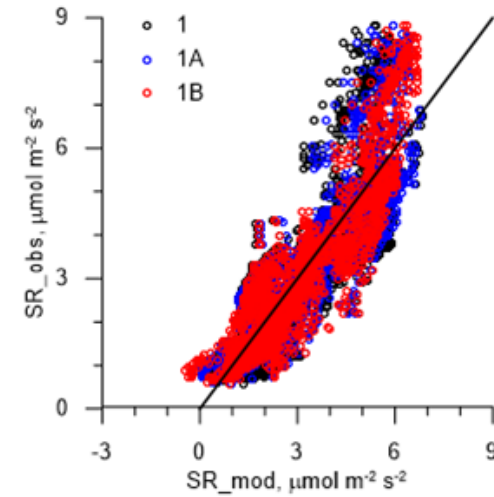
Results – model 3 (exponential)

$$R = r \cdot \exp[k \cdot T_1]$$



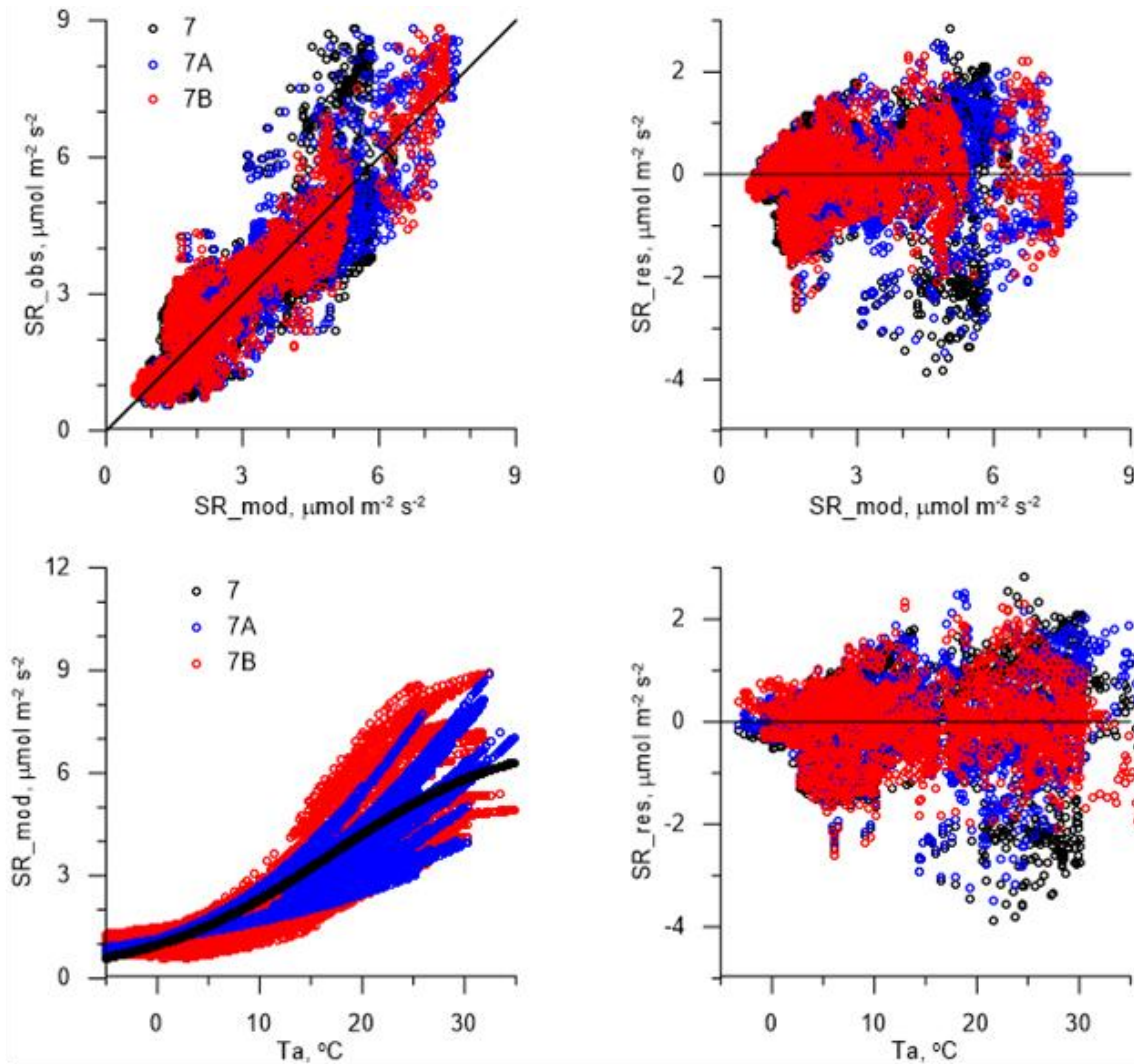
Results – model 1 (linear)

$$R = r + k \cdot T_1$$

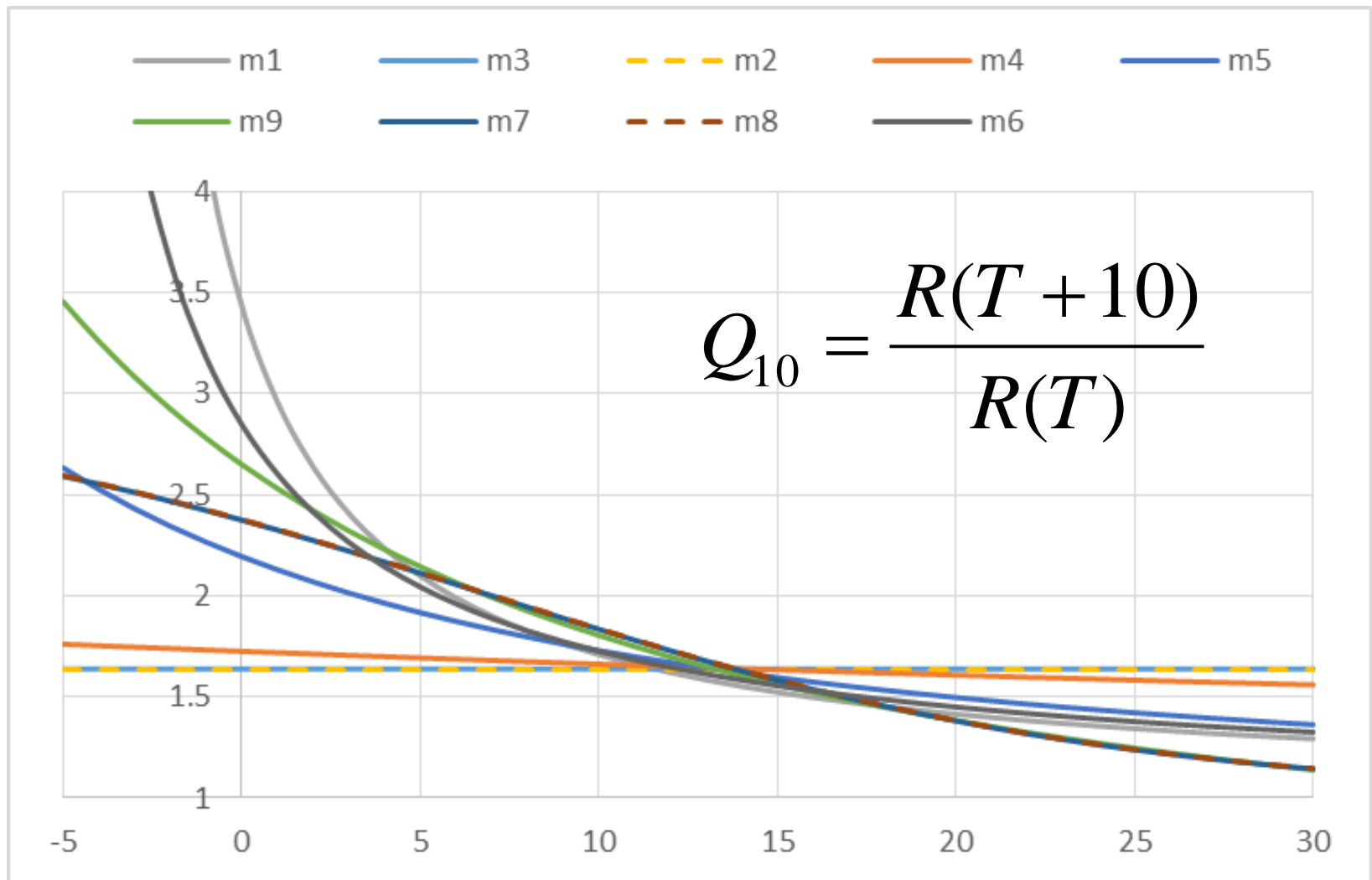


Results – model 7 (logistic)

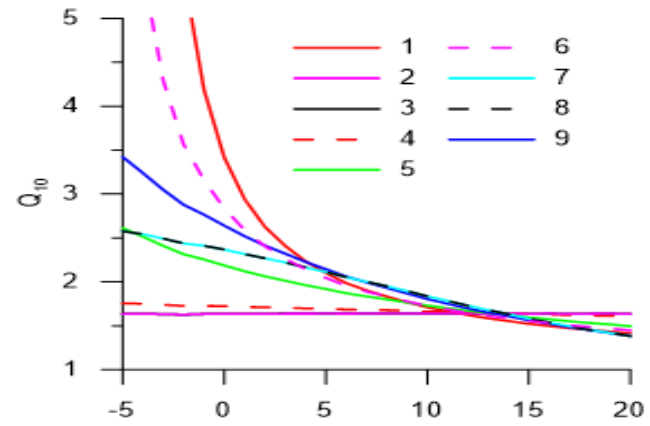
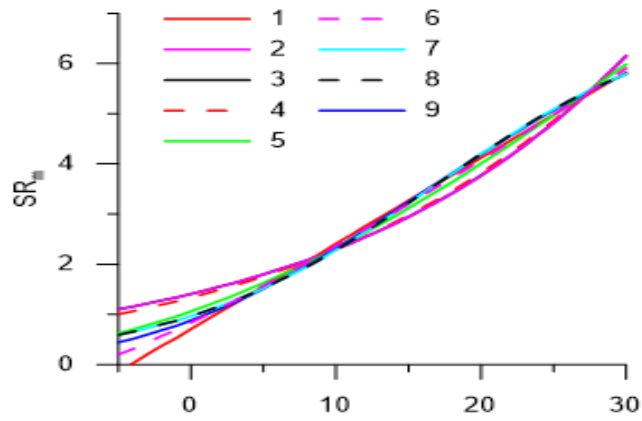
$$R = \frac{r}{1 + p \cdot \exp[-k \cdot T_1]}$$



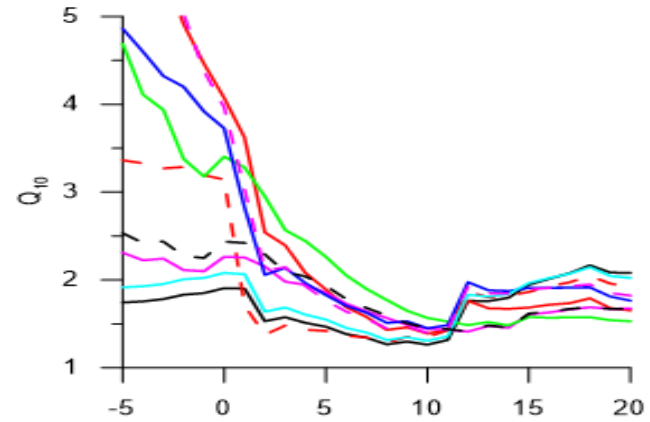
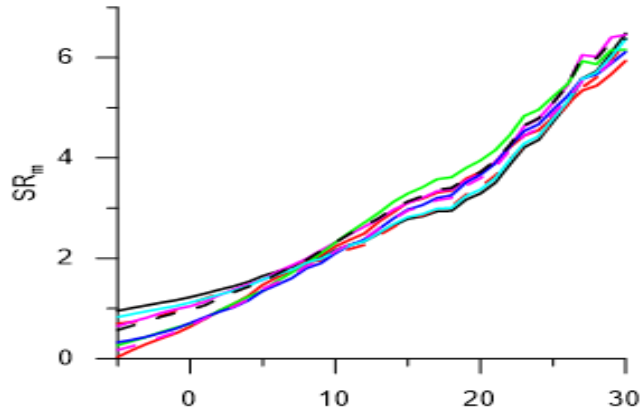
Temperature sensitivity coefficient



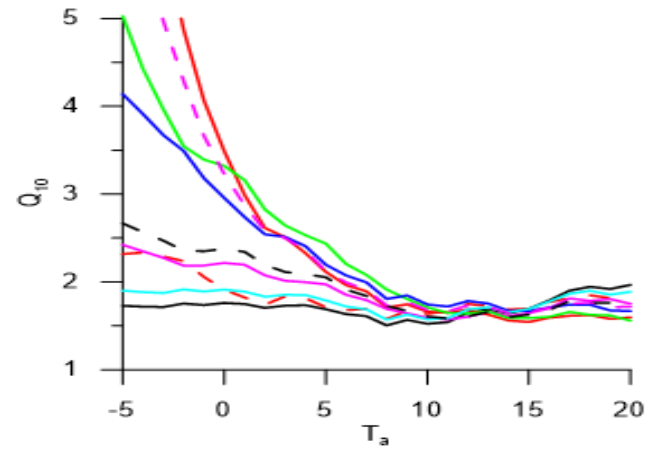
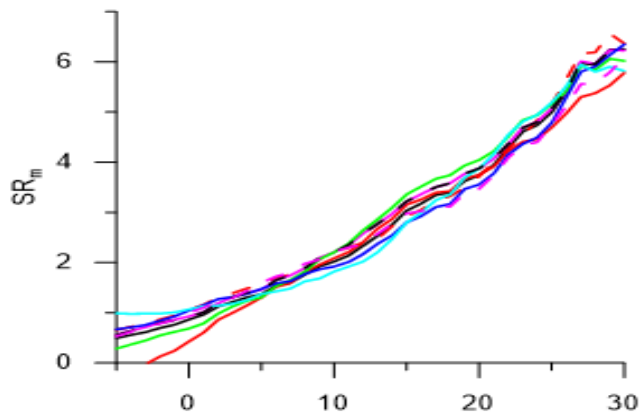
m0



mA



mB



The best soil respiration model

$$SR = \frac{r_0 + r_1 \cdot T_3}{1 + p \cdot \exp[-(k_0 + k_1 \cdot T_2) \cdot T_a]}$$

Model 7B

$T_1 = T_{air}$

$T_2 = T_{20}$

$T_3 = T_{120}$

Спасибо за внимание!